CURRICULUM VITAE

May 31, 2025

Alexander Stoimenow

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20. 05. 1974	Born in Sofia, Bulgaria (Bulgarian citizenship);
08. 1985	Resettlement to Berlin, (former) GDR
30. 06. 1990	Abitur (school-leaving examination) at the Carl-von-Ossietzky-EOS, Berlin
09. 1990 – 09. 1995	Mathematics studies at Humboldt University Berlin (specialization "Ge- ometry" under supervision of Prof Thomas Friedrich), thesis "On Harri- son cohomology and the Drinfel'd conjecture"
11. 07. 1997	B.Sc. degree in Computer science at Humboldt University
10. 1995 – 05. 1998	Promotion (Dr. rer. nat. degree) at Freie Universität Berlin under the su- pervision of Prof. Elmar Vogt. The thesis "On enumeration of chord dia- grams and asymptotics of Vassiliev invariants" has been given the note <i>magna cum laude</i> .
06. 1998 – 03. 1999	Postdoc position at the Mathematics Institute of the Ludwig-Maximilians-University Munich
04. 1999 – 02. 2003	Visitor position at Max-Planck-Institut für Mathematik, Bonn, including
10. 2004 – 04. 2006	JSPS Postdoc fellowship, University of Tokyo
04. 2006 – 11. 2007	COE Program Researcher, Research Institute for Mathematical Sciences, Kyoto University
12. 2007 – 05. 2008	Researcher, Osaka City University Advanced Mathematical Institute
06. 2008 – 02. 2010	BK21 Project Researcher, Department of Mathematical Sciences, KAIST,

Daejeon, Korea

06. 2008 – 02. 2009	Part-time Lecturer, School of Engineering, Information and Communica- tions University, Daejeon, Korea
03. 2010 - 01. 2014	Assistant Professor, Department of Mathematics, Keimyung University, Daegu, Korea
02. 2014 – 02. 2017	Assistant Professor (teaching track), GIST College, Gwangju Institute of Science and Technology, Gwangju, Korea
03. 2017 – 02. 2020	Associate Professor, GIST College, Gwangju, Korea
08. 2020 – 02. 2023	Research Consultant "Computational Knot Theory", School of Comput- ing, KAIST, Daejeon, Korea
03. 2023 – 02. 2028	Dongguk University, WISE campus, Department of Mathematics Educa- tion, visiting research professor

Conferences and talks (incl. scheduled)

July 1995	Ph.D. Summer School on "Geometry and Physics", Odense, Denmark
April 1997	Knot theory workshop in Narbonne, France (talk given)
June 1998	Workshop "Rencontres Dijonnaises autour des nœuds et des tresses", Di- jon, France
August 7-15, 1998	International Knot Theory Meeting "Knots in Hellas, 98", Delphi, Greece (talk given)
June 18-24, 1999	Arbeitstagung MPI Bonn '99
May 24-25, 2000	Clay Institute Millenium Event, Paris, France
June 5-8, 2000	Workshop "Journées Toulousaines autour des tresses et des nœuds" in Toulouse, France
June 18-24, 2000	"Perspectives of Mathematics", Goslar, Germany
March 26 - April 7, 2001	"Symplectic and Contact Topology, Quantum Cohomology, Symplectic Field Theory and Higher-Dimensional Gauge Theory", The Fields Insti- tute, Toronto and the Centre de recherches mathématiques, Montréal
June 15-17, 2002	Canadian Mathematical Society Summer Meeting 2002, Université Laval, Quebec City, Quebec
August 12-16, 2002	Geometric Topology, Satellite Conference of ICM 2002 Beijing, Shaanxi Normal University, Xi'an, China (invited speaker, but could not attend because of lack of travel funding)
July 8-14, 2004	KOOK Seminar International for Knot Theory and Related Topics, Inter- national Conference Center in Awaji-Shima, Japan (talk 'On mutations and Vassiliev invariants (not) contained in knot polynomials')
October 25-27, 2004	Intelligence of Low Dimensional Topology 2004, Osaka City University (talk 'The second coefficient of the Jones polynomial')

December 23-26, 2004	Topology of Knots, Tokyo Woman's Christian University
February 12-14, 2005	Tohoku Knot Seminar in Akita, ALVE, Akita-shi, Japan (talk 'Burau representation and braid index')
August 1-6, 2005	The Second East Asian School of Knots and Related Topics in Geomet- ric Topology, Dalian University of Technology, Dalian, China (talk 'The existence of achiral knot diagrams')
August 28 - September 1,	2005 "Geometry and Algebra of Knots and manifolds", Konan Univer- sity, Kobe city, Japan
October 12-14, 2005	Knot Seminar (-in Zao-), Yamagata Zao, International Zaokoegen Ho- tel (talk 'Concordance and Thurston-Bennequin invariants of posi- tive/negative knots and links')
December 23-26, 2005	Topology of Knots VIII, Waseda University, Tokyo (talk 'Weight sys- tems of trivalent graphs and hyperbolic volume of alternating knots by genus')
February 17-20, 2006	Hiroshima Topology Conference (Celebrating Prof. Takao Matumoto's 60th birthday), Hiroshima University, Higashi-Hiroshima city, Japan
July 22-27, 2006	Intelligence of Low Dimensional Topology 2006, Hiroshima University, Higashi-Hiroshima city, Japan (talk 'Mutation and the colored Jones polynomial')
September 13-15, 2006	Groups of Diffeomorphisms 2006 (Celebrating Prof. Shigeyuki Morita's 60th birthday), University of Tokyo, Japan
February 5-8, 2007	The Third East Asia School of Knots and Related Topics, Osaka City University (talk 'Alexander polynomials, minimal genus, and fibering of arborescent links')
May 10-25, 2007	Workshop "Link homology and categorification", Department of Mathe- matics and RIMS, Kyoto University
July 6-8, 2007	Jubilee International Conference "New Trends in Mathematics and In- formatics", 60 years Institute of Mathematics and Informatics, Bulgar- ian Academy of Sciences (talk 'Hecke algebra representations of braid groups and a conjecture of Jones')
September 5-7, 2007	Topology and Computer 2007, Akita University (talk 'Genus minimality of canonical surfaces and Alexander polynomial of canonical fiber sur- faces')
September 11-14, 2007	Workshop "Low Dimensional Topology and infinite Dimensional Ge- omerty", University of Tokyo, Tanbara House
December 22-25, 2007	Topology of Knots X, Tokyo Woman's Christian University (talk 'Hecke algebra representations of braid groups and a conjecture of Jones')
January 23, 2008	The Fourth East Asia School of Knots and Related Topics, University of Tokyo, Japan (talk 'Determinants of knots and Diophantine equations')
August 12 -14, 2008	The First Topology Workshop KAIST (talk 'Lie groups, Burau represen- tation, and non-conjugate braids with the same closure link')

January 12-15, 2009	The Fifth East Asia School of Knots and Related Topics, Gyeongju, Korea (talk 'Lie groups, Burau representation, and non-conjugate braids with the same closure link')
March 19 - 21, 2009	Low dimensional topology and knot theory workshop, "Swiss Knots 2009", Fribourg, Switzerland
April 25, 2009	KMS Meeting, Aju University, Suwon, Korea (talk 'The Satellite crossing number conjecture for cables of knots')
August 17 -19, 2009	The Second Topology Workshop KAIST
September 5 - 10, 2009	9th International Conference on Geometry and Applications, Varna, Bul- garia (talk 'Non-conjugate braids with the same closure link')
December 16 - 20, 2009	Joint Meeting of the Korean Mathematical Society (KMS) and the Amer- ican Mathematical Society (AMS), Special Session on Knot Theory and Related Topics, Ewha Womans University, Seoul, Korea (talk 'On non- conjugate braids with the same closure link')
January 11 - 13, 2010	8th Geometric topology fair, KAIST, Mathematics department (talk 'Around Bennequin's inequality')
April 24, 2010	Spring Meeting of the Korean Mathematical Society, Chungnam National University, Daejeon, Korea
June 19, 2010	Annual meeting of Yeungnam Mathematical Society, Yeungnam Univer- sity, Kyungsan, Korea (talk 'On non-conjugate braids with the same clo- sure link')
March 18, 2011	Knots and Spatial Graphs 2011 Workshop, KAIST, Mathematics depart- ment
March 20-25, 2011	Spring School in Geometry and Quantum Topology, Les Diablerets, Switzerland
April 28, 2012	Spring Meeting of the Korean Mathematical Society, Seokmyeong Wom- ans University, Seoul, Korea (talk 'Roots of the Alexander polynomial and Hoste's conjecture')
July 27, 2012	2012 TAPU Workshop on Knot Theory and Related Topics, Pusan Na- tional University, Busan, Korea (talk 'Diagram genus, generators and ap- plications')
August 17, 2012	Knots and Spatial Graphs 2012 Workshop, KAIST, Mathematics depart- ment (talk 'Everywhere Equivalent and Everywhere Different Knot Dia- grams')
October 25, 2013	2013 KMS Annual Meeting, The University of Seoul
November 9, 2013	60th KPPY Combinatorics Workshop, Kyungpook National University, Daegu (talk 'On dual triangulations of surfaces')
February 10-14, 2014	China-Korea Workshop on Low Dimensional Topology in Shanghai, East China Normal University, Shanghai, China (talk 'On dual triangulations of surfaces')
July 7-10, 2014	International Conference "Mathematics Days in Sofia", Bulgarian

Academy of Sciences, Sofia, Bulgaria

August 13-21, 2014 ICM 2014, Coex, Seoul August 22-24, 2014 Knots and Low Dimensional Manifolds, Satellite Conference of Seoul ICM 2014, BEXCO Convention & Exhibition Center, Busan, Korea, talk "Concordance of positive knots" October 31, 2014 GIST Foreign Faculty Workshop, GIST College, talk "Academic (Written) Communication" December 6, 2014 67th KPPY Combinatorics Workshop, Kyungpook National University, Daegu (talk 'On dual triangulations of surfaces II') April 24-26, 2015 Spring meeting of Korean Mathematical Society, Pusan National University, Korea May 2, 2015 Topology Workshop in Honor of Prof. Gyo Taek Jin's 60th birthday, KAIST, Daejeon, Korea Knots and Spatial Graphs 2015 Workshop, Dept. of Mathematical Sci-November 5-7, 2015 ences, KAIST (talk 'Roots of the Alexander polynomial and Hoste's conjecture') June 25-27, 2016 Workshop on Graphs and Knots, School of Mathematical Sciences, Xiamen University, China (talk 'Coefficients and non-triviality of the Jones polynomial') International Conference on Low-Dimensional Topology Knots in Hel-July 16-23, 2016 las 2016, International Olympic Academy, Ancient Olympia, Greece (talk 'On coefficients and roots of the Alexander-Conway polynomial') October 20-23, 2016 International Conference for the 70th Anniversary of the Korean Mathematical Society, Seoul National University, Korea May 15-19, 2017 Quantum Topology and Geometry in Toulouse, Université Paul Sabatier, Toulouse, France July 10-14, 2017 "Mathematics Days in Sofia, 2017", Bulgarian Academy of Sciences, Sofia, Bulgaria April 21, 2018 KMS Meeting, Kyeonghee University, Seoul, Korea 4th Mini Workshop on Knot Theory, Dongguk University Gyeongju, Ko-June 7-8, 2019 rea (talk 'Exchange moves and non-conjugate braid representatives of links') July 15, 2019 Geometry and Mathematical Physics, Workshop dedicated to the memory of Vasil Tsanov, held at University of Architecture, Civil Engineering and Geodesy (UACEG), Sofia, Bulgaria October 24-27, 2019 KMS Fall Meeting, Hongik University, Seoul, Korea November 8-11, 2019 The Third Pan Pacific International Conference on Topology and Applications (PPICTA), Sichuan University, Chengdu, China (talk 'Exchange moves and non-conjugate braid representatives of links') Knots and Spatial Graphs 2020, A workshop in memory of Choonbae February 17-18, 2020 Jeon, KAIST

- February 1-3, 2021 Knots and Spatial Graphs 2021, online workshop, organized by Gyongju Gongkuk Uni. (talk 'Knot polynomial computation and application to braid index')
- June 25-27, 2021 KSIAM (The Korean Society for Industrial and Applied Mathematics) 2021 Spring conference, Gangneung TopsTen Hotel (Online Participation)
- June 27-July 1, 2022 Computing in topological structures: Foundations imand Sirius plementations, Mathematics Center, Sochi, Russia crossing (Online talk 'Odd number amphicheiral knots') https://sites.google.com/view/cts-2022/home/invited-speakers
- February 6-9, 2023 East Asian Conference on Geometric Topology 2023, Online Hosted by Soochow University, China (Online talk 'Strong quasipositivity of links')
- June 15-17, 2023 "Knots and Spatial Graphs 2023" Workshop, KAIST, Department of Mathematical Sciences (talk 'Strong quasipositivity of links').
- September 25-29, 2023 CCC 2023 "Continuity, Computability, Constructivity: From Logic to Algorithms", RIMS, Kyoto University, Japan (online participation)
- October 27-28, 2023 Fall Workshop on Algorithms & Computation, Postech, https://algo.postech.ac.kr/workshops/fwac23/
- December 11-15, 2023 Winter School on Low-dimensional Topology and Related Topics IBS POSTECH Campus Bldg. #301 (talk 'Burau representation, stabilization and exchange moves of braids' December 12, 2023)
- April 18-20, 2024 KMS Spreing Meeting, Daejeon Convention Center and KAIST, Daejeon (talk 'Strong quasipositivity and arc index', April 19)
- June 5-14, 2023 2024 MATRIX-IBSCGP Workshop on Symplectic and Low-dimensional Topology, IBS POSTECH Campus Bldg. #301
- September 30-October 4, 2024 tumn School on Low-Dimensional topology and related topics, IBS POSTECH Campus Bldg. #301
- November 4-8, 2024 Knots and Spatial Graphs 2024 UAE United Arab Emirates University, Al Ain (UAE) (talk 'Strong quasipositivity and arc index', Nov. 5)
- February 2-6, 2025 The First International Online Knot Theory Congress, in honor of Lou Kauffman's 80th anniversary (talk 'Strong quasipositivity, Thurston-Bennequin invariants, and arc index' https://www.youtube.com/watch?v=p2sK5oJZNjU)
- March 19, 2025 Mini-Workshop on Computation, Informatics Dept, KAIST, https://kaist.theoryofcomputation.asia/seminars#section2025. (Talk 'Integer factorization of matrices and 4-dimensional genera of knots')

Seminar talks (outside conferences)

"Some applications of link polynomial evaluations" (Vortrag am Graduiertenkolleg University Bonn, 11/6/1999)

"Wheel graphs, Lucas numbers and the determinant of a knot" (MPI-Oberseminar, 30/3/2000)

"On the number of links and link polynomials" (Oberseminar Topologie, MPI, 11/12/2000)

"Canonical genus and the signature" (Kobe Topology Seminar, Kobe University, Novenber 24, 2001)

"Special diagrams and the positivity of the signature" (Nara Topology Seminar, Nara Women's University, November 29, 2001)

"On the signature of positive links" (Mathematics Institute Seminar, University Bonn, 19/4/2002, and Oberseminar Topologie, MPI, 13/1/2003, Topology Seminar Université Lille, 14/11/2003)

"On some relations between hyperbolic volume and combinatorial knot invariants" (Topology seminar, University of Toronto, 26/3/2003)

"Square Fibonacci numbers and linear recurrence sequences" (Graduate seminar, University of Toronto, 17/4/2003)

"Four Color Theorem, Lie Algebras, hyperbolic volume and enumeration of alternating knots by genus" (Topology Seminar, Tokyo Institute of Technology, 3/3/2004)

"On mutations and Vassiliev invariants (not) contained in knot polynomials" (Friday seminar on Knot Theory, Osaka City University, 11/6/2004)

"Properties of closed 3-braids" (Topology Seminar, University of Tokyo, 30/11/2004)

"Properties of closed 3-braids" (KOOK Seminar, Osaka City University, 2/4/2005)

"Applications of braiding sequences" (Research Institute for Mathematical Sciences, Topology Seminar, 17/11/2005)

"Braiding sequences and Thurston-Bennequin invariants" (Hokkaido University, Department of Mathematics Colloquium 21/12/2005)

"Knots and their crossing numbers" (Research Institute for Mathematical Sciences, Colloquium, 10/5/2006)

"Estimation of crossing numbers of knots" (Research Institute for Mathematical Sciences, Topology Seminar, 13/7/2006)

"Bennequin surfaces and braid index of alternating knots" (Friday Seminar on Knot Theory, Osaka City University, 13/10/2006)

"Hecke algebra representations of braid groups and a conjecture of Jones" (Topology Seminar, University of Geneva, 18/10/2007)

"Determinants of knots and Diophantine equations" (Topology Seminar, ETH Zurich, 22/10/2007)

"Knots and crossing numbers" (Kyoto University International Researchers Monthly Seminar, Kyoto University International Office, January 11, 2008)

"Vassiliev invariants, Seifert matrix, and hyperbolic volume of knots" (Friday seminar on knot theory, Osaka City University, February 22, 2008)

"Mutation and the colored Jones polynomial" (Topology Seminar, University of Geneva, 22/5/2008; Topology Seminar, KAIST, 16/6/2008)

"Computing cabled knot polynomials and deciding mutation", "Computing link polynomials with the Millett-Ewing programs" (Topology Seminar, KAIST, 30/6/2008, 8/7/2008)

"Tait's Conjectures and odd crossing number amphicheiral knots" (BK21 Seminar, KAIST, 16/3/2009)

"Around Bennequin's inequality" (Korea University, Seoul, 15/5/2009)

"Distinguishing polygonal knots" (Korea Science Academy KSA of KAIST Undergrad student Seminar, KAIST, 28/7/2009)

"Signature and concordance of positive links" (POSTECH, Pohang, Korea, 26/8/2009)

"On roots of the Alexander polynomial" (NRF grant Research Seminar, Keimyung University, 23/9/2011 and KAIST, 28/10/2011)

"Diagram genus, generators and applications" (Topology Seminar, Durham University, 19/1/2012)

"Roots of the Alexander polynomial and Hoste's conjecture" (Topology Seminar, University of Glasgow, 23/1/2012)

"Diagram genus, generators and applications II" (Algebra Seminar, Newcastle University, 24/1/2012)

"Roots of the Alexander polynomial and Hoste's conjecture" (Topology Seminar, Pusan National University, 22/5/2012)

"Everywhere equivalent and everywhere different knot diagrams" (NRF grant Research Seminar, KAIST, 8/6/2012)

"Minimal genus and fibering of canonical surfaces" (NRF grant Research Seminar, KAIST, 24/11/2012)

"Hyperbolicity of the canonical genus two knots" (NRF grant Research Seminar, Andong, 6/4/2013)

"On roots and coefficients of the Alexander polynomial" (Topology Seminar, University of Geneva, 11/7/2016)

"Coefficients and Non-Triviality of the Jones Polynomial", "On dual triangulations of surfaces" (Topology Seminar, KIAS, Seoul, 25/9/2016)

"Solved and unsolved mysteries of numbers", GIST GIP (Global Intern Program) exchange student seminar, 4/8/2017

"Exchange moves and non-conjugate braid representatives of links" (Topology Seminar, University of Melbourne, 27/9/2018, and Topology Seminar, Monash University, 4/10/2018)

"Exchange moves and non-conjugate braid representatives of links" (Topology Seminar, Pusan National University, 5/4/2019)

"Exchange moves and non-conjugate braid representatives of links" (TU Berlin, Discrete Mathematics / Geometry, online seminar, 11/24/2021) https://www.tu-berlin.de/?id=138801

"Exchange moves and non-conjugate braid representatives of links" (NU Singapore Topology and Geometry, online seminar, 8/11/2022)

"Burau Representation and Application to Reducibility and Exchangeability of Braids" (General seminar of the section "Analysis, Geometry and Topology" and seminar of the section "Algebra and Logic" Institute of Mathematics and Informatics - Bulgarian Academy of Sciences 26 September 2023)

"Diagram genus, generators and applications" (CGP Seminar IBS POSTECH, 10/25/2023)

"평면 수직 다변형의 엇갈림 수" (Dongguk Student Math Seminar, 24 April 2024)

"Implementation of the Burau spectral test", joint with Jaden Jorradol (School of Computing, KAIST), seminar on Exact Real Computation, School of Computing, KAIST, 4 June 2024, see https://youtu.be/Xbk4a_cQLEc

"The Alexander polynomial of planar even valence graphs", "Semiadequacy properties for the edge Jones polynomial coefficients", Math department, Chinese University of Hong Kong, Feb 27, Mar 3, 2025

"Introduction to Knots", "Introduction to 4-dimensional Genera" Math department, Sofia University, Apr 4,7, 2025 (in Bulgarian) https://youtu.be/nWQ3DbHvzJE, https://youtu.be/eVayvVknTLE

Trustworthy AI

"Software Engineering for Machine Learning" (joint with M. Ziegler, SNU Trustworthy AI Lab meeting, 1/9/2023), https://www.youtube.com/watch?v=HvGCaRmFUIQ

Lectures (incl. series of talks and minicourses)

"Non-associative tangles" (following a paper of D. Bar-Natan, "Geometric topology, Proceedings of the Georgia international topology conference", W. H. Kazez, ed., 139-183, Amer. Math. Soc. and International Press, Providence, 1997), Lecture series, knot theory seminar, Humboldt University Berlin, 1993/1994.

"Algebraic structures on modules of diagrams" (following P. Vogel's preprint, published far later in Journal of Pure and Applied Algebra, **215(6)** (2011), 1292–1339), Lecture series, knot theory seminar, Humboldt University Berlin, 1994/1995.

"Some applications of braiding sequences", series of 4 talks: "A bound for the number of restricted Vassiliev invariants", "The canonical genus" (2 talks), "On the crossing number of semiadequate links", Low dimensional topology Seminar, Research Institute for Mathematical Sciences, Kyoto University, November 16, 17, 30, 2001.

"Mathematical English" (rules of writing mathematical papers in English), Osaka City University, June 10, 17, 24, July 1, 2004

Computing school seminar Prof. Ziegler, KAIST "Introduction to Computational Knot Theory" (9/14/2020), https://www.youtube.com/watch?v=jSn30jBA3R8, "Knotscape and knot tables" (11/12/2020), https://www.youtube.com/watch?v=2_33U4Rdx5c

Teaching

(All courses 3 credit hours / week, recitation 1 credit hour / week)

Summer 2008

Ordinary Differential Equations, School of Engineering, Information and Communications University

Fall 2008

Calculus II, ibid.

Spring 2010

Mathematical English, Department of Mathematics, Keimyung University Linear Algebra (4th grade), Department of Game and Mobile Technology, Keimyung University

Fall 2010

Mathematical English, Department of Mathematics, Keimyung University Linear Algebra (1st grade), Department of Game and Mobile Technology, Keimyung University Discrete Mathematics, Department of Microsoft IT, Keimyung University Calculus and Applications (Pre-calculus), Department of Mathematics, Keimyung University

Spring 2011

Calculus and Applications (Pre-calculus), Department of Mathematics, Keimyung University Vector Analysis, Department of Mathematics, Keimyung University

Fall 2011

Calculus (1st grade), Department of Mathematics, Keimyung University Mathematical English, Department of Mathematics, Keimyung University Teaching Practice, Department of Mathematics Education, Keimyung University Calculus (2nd grade), Keimyung Adams College, Keimyung University

Spring 2012

Calculus and Applications (4th grade), Department of Mathematics, Keimyung University Linear Algebra (2nd grade), Department of Mathematics, Keimyung University Vector Analysis (4th grade), Department of Mathematics, Keimyung University

Fall 2012

Vector Analysis II (2nd grade), Department of Game and Mobile Technology, Keimyung University Mathematical English, Department of Mathematics, Keimyung University Calculus (2nd grade), Keimyung Adams College, Keimyung University

Spring 2013

Vector Analysis I (2nd grade), Department of Game and Mobile Technology, Keimyung University Mathematical English, Department of Mathematics, Keimyung University Calculus and Applications (4th grade), Department of Mathematics, Keimyung University

Fall 2013

Vector Analysis II (2nd grade), Department of Game and Mobile Technology, Keimyung University Calculus (2nd grade), Keimyung Adams College, Keimyung University

Spring 2014

Single Variable Calculus and Applications (1st grade), GIST College (2 sections + 2 recitations) Introduction to Linear Algebra & Applications (2nd grade), GIST College (1 section + recitation)

Fall 2014

Multivariable Calculus and Applications (1st grade), GIST College (2 sections + 2 recitations) Introduction to Linear Algebra & Applications (2nd grade), GIST College (1 section + recitation)

Spring 2015

Single Variable Calculus and Applications (1st grade), GIST College (2 sections + 2 recitations) Introduction to Linear Algebra & Applications (2nd grade), GIST College (1 section + recitation)

Fall 2015

Multivariable Calculus and Applications (1st grade), GIST College (2 sections + 2 recitations) Introduction to Linear Algebra & Applications (2nd grade), GIST College (1 section + recitation)

Spring 2016

Single Variable Calculus and Applications - Honors (1st grade), GIST College (2 sections + 2 recitations)

Introduction to Linear Algebra & Applications (2nd grade), GIST College (1 section + recitation)

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Fall 2016

Multivariable Calculus and Applications (1st grade), GIST College (2 sections) Introduction to Linear Algebra & Applications (2nd grade), GIST College (2 sections)

Spring 2017

Single Variable Calculus and Applications - Honors (1st grade), GIST College (2 sections) Introduction to Linear Algebra & Applications (2nd grade), GIST College (2 sections)

Fall 2017

Multivariable Calculus and Applications (1st grade), GIST College (2 sections + 2 recitations) Introduction to Topology (4th grade), GIST College

Spring 2018

Single Variable Calculus and Applications - Honors (first grade), GIST College (1 section + recitation)

Introduction to Linear Algebra & Applications (second grade), GIST College (2 sections + 2 recitations)

Fall 2018

Introduction to Linear Algebra & Applications (2nd grade), GIST College (2 sections + 2 recitations) Introduction to Topology (4th grade), GIST College

Spring 2019

Single Variable Calculus and Applications (first grade), GIST College (1 section + recitation)

Introduction to Differential Equations & Applications (second grade), GIST College (2 sections + 2 recitations)

Fall 2019

Introduction to Linear Algebra & Applications (2nd grade), GIST College (2 sections + 2 recitations) Introduction to Topology (4th grade), GIST College

Spring 2021

CS300 Introduction to Algorithms (Chapter 2a-c 3a-b), School of Computing, KAIST https://www.youtube.com/watch?v=Nkwy7jhyLkQ(2a) http://youtu.be/qLuryM20Zz4/(2b)

Fall 2021

CS300 Introduction to Algorithms (Chapter 2, 3), School of Computing, KAIST https://www.youtube.com/playlist?list=PLvcvykdwsGNF9nmJpwXJklSCzstnFlNik

Supervision

1-year research project: Jihoon Hyun (School of Computing, KAIST) 1-semester project (2024/1)

"Implementation of the Burau spectral test using exact real computation": Jaden Jorradol (School of Computing, KAIST),

technical report: https://cs.kaist.ac.kr/research/techReport, CS-TR-2024-428
presentation: https://www.youtube.com/watch?v=Xbk4a_cQLEc,
at the Conference "(CCC'2024) Continuity, Computability, Constructivity From Logic to Algorithms" Nice (France) (https://www.lix.polytechnique.fr/CCC2024/i.php?n=Main.Cfp)

Invitations and Working visits

April 1996	Strassbourg (France), C. Kassel
June 1996	Toulouse (France), T. Fiedler
March 1999	Toulouse, T. Fiedler
June 1999	Zurich, V. Chernov
November 1999	Institut des Hautes Études Scientifiques in Bures-sur-Yvette (France)
January-July 2001	University of Toronto, Kunio Murasugi
November 2001	Research Institute for Mathematical Sciences, Kyoto University (Japan), Hitoshi Murakami
May 2003	Toulouse, T. Fiedler
October 2003	Waterloo (Canada), L. Kauffman
November 2003	Lille (France), S. Kallel; Toulouse, T. Fiedler
February-March 2004	Tokyo Institute of Technology, Hitoshi Murakami
June-July 2004	Osaka City University, Akio Kawauchi

October 2007	ETH Zurich, Sebastian Baader; University of Geneva, Van Quach
May 2008	University of Geneva, Van Quach
January 2012	Newcastle University, Alina Vdovina
January-February 2015	Mebourne University, Hyam Rubinstein
July 2015	University of Geneva, Van Quach and University of Bern, Sebastian Baader
July 2016	University of Geneva, Van Quach and University of Bern, Sebastian Baader
September/October 2018	³ University of Melbourne, Hyam Rubinstein and Monash University, Jessica Purcell
February/March 2025	Chinese University of Hong Kong, Zhongtao Wu (吳忠濤)
April 2025	Sofia UNiversity, Krassimira Vlachkova

Research grants

4/2007-3/2009	2-year individual research grant from Ministry of Science and Education, "Polynomial invariants of knots and related theory", Japan (managed by RIMS, Kyoto and Osaka City University), 若手研究 (B), Nr. 19740035, JPY 1,510,000
9/2011-8/2014	3-year group research project from NRF, Korea (managed by KAIST), "Computational approach toward geometric and combinatorial proper- ties of knots", NRF-2011-0027989, 600,000,000KRW
6/2013-5/2014	1-year individual research grant from NRF, Korea (managed by Keimyung University), "Combinatorial knot theory related to polynomial invariants", Nr. 2013-0366, 19,350,000원
3/2021-12/2021	1-year International Collaboration Signature Project in 2021 "Compu- tational Knot/Braid Theory" (managed by Prof. Ziegler's KAIST lab.) 5,000,000 KRW
3/2023-2/2028	5-year group research project from NRF, Korea (managed by Dongkuk University), "Strongly quasipositive knots and arc index", 2023R1A2C1003749, 600,000,000 KRW

Awards

Excellent Research Achievement Award, Keimyung University, May 2012

Administrative matters

Organizer: Graduate Student Seminar, Mathematics Institute, Ludwig-Maximilians-University Munich, 06. 1998 – 03. 1999

Co-Organizer: International Faculty Workshop, GIST College, October 31-November 1, 2014

Session Chairman: International Graduate Course Student Workshop for Knot Theory and Related Topics, Osaka City University, Media Center, July 5-7, 2004; Tohoku Knot Seminar in Akita, ALVE, Akita-shi, Japan, February 12-14, 2005. Workshop on Graphs and Knots, School of Mathematical Sciences, Xiamen University, China, June 25-27, 2016

Organizer: Online workshop on "Computational Knot Theory", KAIST, May 26-June 2, 2021, http://www.stoimenov.net/stoimeno/homepage/ckt/

Mini-Workshop "Knots + More", KAIST, August 18th-25th, 2021, http://www.stoimenov.net/stoimeno/homepage/kam/

Co-Organizer: "Knots and Spatial Graphs 2023" Workshop, KAIST, June 15th-17th, 2023

Memberships in Professional Societies

Korean Mathematical Society KMS (2009-present), German Mathematical Society DMV (2023-)

Other academic activities

Contributing Visitor, Trustworthy AI Lab, Graduate School of Data Science, Seoul National University, https://trustworthyailab.snu.ac.kr/

Refereeing

Journals (a substantiated, but not entirely complete list of those having directed evaluation queries to me, regardless of what or how detailed comments I have provided)

Topology, Compositio Mathematica, Documenta Mathematica, J. of Knot Theory and Its Ramifications, Algebr. Geom. Topol., Pacific J. Math., Topology and its Applications, Math. Proc. Camb. Phil. Soc., International Mathematics Research Notices, Geometriae Dedicata, SIGMA (Symmetry, Integrability and Geometry: Methods and Applications), Discrete Mathematics, Indiana University Mathematics Journal, Mathematische Annalen, Abstract and Applied Analysis, Journal of Symbolic Computation, Proceedings of Amer. Math. Soc., Bull. London Math. Soc., Proc. London Math. Soc., Electronic Journal of Combinatorics, European Journal of Combinatorics, Journal of Topology, Journal of Applied Analysis, Internat. J. Math., Revista Matemática Iberoamericana

Social sci.: Aslib Journal of Information Management, International Journal of Science Education Part B: Communication and Public Engagement, Journal of Academic Ethics

General sci.: Heliyon

Organizations and Services

Online Review: AMS Math Reviews, Zentralblatt,

Grant Proposals: National Science Foundation (US), United Arab Emirates University (UAE)

Others

Inclusion in Marquis "Who's Who in the World" 2010 Edition

Supervision of English Study Groups (K-Circle), Fall semester 2010, spring and fall semester 2011, Keimyung University

3rd Prize, Photography contest, Keimyung University, May 2012

Language skills

Russian (Intermediate), English (Fluent), German (Fluent), Korean (Advanced) (2014.02.17 TOPIK 33 회 2급합격, 자격증번호 0120120028, 취득기관 TOPIK KOREA), Japanese (Intermediate)

Publications

Degree theses

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- [St2] On enumeration of chord diagrams and asymptotics of Vassiliev invariants, Doctor thesis, Freie University Berlin, 1998.

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1 Subject and Achievement of past Research

My research covers several areas of knot theory, with relations to combinatorics, number theory and algebra, which are outlined below (and by no means unrelated). The following explains some key topics, with reference to *published or accepted* papers (cf. the bibliography in "Publications") when available.

1.1 Vassiliev invariants

My first work was to improve the upper bound on the dimension of Vassiliev invariants of degree D. The best known previous upper bound was (D-2)!/2 due to Ng. It was known that Vassiliev invariants can be understood combinatorially in terms of chord diagrams modulo the 4T relation. I introduced a certain type of chord diagrams and showed that they generate modulo 4T relations the space of Vassiliev invariants. Then I estimated from above the number of such chord diagrams to $D!/1.1^D$ [St3]. Later, Zagier [Za] showed that the generating series of the numbers of such chord diagrams occurs in a strange identity related to the Dedekind eta-function. He found the exact asymptotical behaviour of these numbers, improving the number 1.1 to $\pi^2/6$, thus establishing the currently best upper bound.

My later work were constructions of knots with Vassiliev invariants of bounded degree and specific properties, like given unknotting numbers, signatures and 4-genera [St19]. I showed the nonexistence of Vassiliev invariants that depend on any finite number of link polynomial coefficients (except the Conway/Alexander polynomial) [St64].

1.2 Legendrian knots

Legendrian knots are called knots embedded in the standard contact space. There are inequalities relating the Thurston-Bennequin invariant and Maslov number of Legendrian knots and the degrees of the polynomial invariants of the underlying topological knots. Using these inequalities I gave estimates of the invariants of Legendrian negative knots [St15, St27]. This result can be considered as a generalization of Kanda's determination of the maximal Thurston-Bennequin invariant of the negative trefoil.

1.3 Gauss diagram formulas

Fiedler and Polyak-Viro introduced a new approach to defining Vassiliev invariants by explicit formulas. Such formulas involve sums over specific tuples of crossings of a knot or link diagram of functions involving writhes of the crossings (similarly to linking numbers). These formulas proved useful in the study of positive knots (knots with diagrams all of whose crossings are positive). Positive knots and links have been studied, beside because of their intrinsic knot-theoretical interest, with different motivations and in a variety of contexts, including singularity theory, algebraic curves, dynamical systems, and (in some vague and yet-to-be understood way) in 4-dimensional QFTs. Using the Fiedler-Polyak-Viro formulas, I found several inequalities between Vassiliev invariants of positive knots, allowing to exclude certain knots from having this property [St12]. Later I sought generalizations of some criteria to almost positive knots [St15].

1.4 Canonical Seifert surfaces

The set of knot diagrams whose canonical Seifert surfaces (that is, surfaces obtained by Seifert's algorithm) of given (canonical) genus admits a structure of generating series. One of the first insights was, for example, that the number of alternating knots of fixed genus grows polynomially in the crossing number [SV, St17].

This approach allows one to prove much more, and has developed into a quite large body of work. Centrally, it is described in my book [St91]. While it is meant as a research monograph, it can be approached on a rather non-exprest level. It contains a general introduction, then the presentation and proof of several results (mainly the description of genus 4 generating series and its application), and concludes with a summary of further directions of related research. There is a series of further articles; for example, see [St69] for an application to concordance.

1.5 Non-trivial Jones polynomial problem

In 1985 Jones discovered the famous polynomial invariant named after him and asked if it distinguishes all non-trivial knots from the trivial one. His question remains unanswered despite the recent (negative) solution for links. I showed that semiadequate links, as defined by Lickorish-Thistlethwaite, have non-trivial Jones polynomial. Montesinos links are semiadequate, and then I showed that so are 3-braid links, so the non-triviality result applies to these classes.

1.6 Odd crossing amphicheiral knots

A major application of the method for showing non-trivial Jones polynomial is the proof thet for every odd number $n \ge 15$, there is a prime amphicheiral knot of crossing number n [St86]. This problem goes back to the beginnings of knot theory with Tait in the late 19th century. A survey can be found in [St60].

1.7 Mutation and the colored Jones polynomial

In joint work with Toshifumi Tanaka [ST], we found examples of knots with the same polynomial invariants and hyperbolic volume, with variously coinciding 2-cable polynomials and colored Jones polynomials, which are not mutants. In particular, we show that there exists an infinite family of pairs of hyperbolic knots with equal colored Jones polynomial, which are not mutants. This answers a question of Przytycki.

1.8 Closed 3-braids

I classified among closed 3-braid links the alternating [St40], braid positive, strongly quasipositive and fibered ones. Then I showed that 3-braid links with given (non-zero) Alexander or Jones polynomial are finitely many, and can be effectively determined. In recent joint work with M. Hirasawa and M. Ishiwata we showed that 3-braid links have a unique incompressible Seifert surface.

1.9 Roots of the Alexander polynomial and Hoste's conjecture

The Alexander polynomial remains one of the most fundamental invariants of knots and links in 3-space. It topological understanding has led a long time ago to the insight what (Laurent) polynomials occur as Alexander polynomial of an arbitrary knot. Ironically, the question to characterize the Alexander polynomials of alternating knots turns out to be far more difficult, even although in general alternating knots are much better understood. Hoste, based on computer verification, made the following conjecture about 10 years ago: If *z* is a complex root of the Alexander polynomial of an alternatingknot, then $\Re e z > -1$. In [St74] I obtain some results toward this conjecture, about 2-bridge (rational) knots or links, 3-braid alternating links, and Montesinos knots. For its relation to (or rather, independence from) other properties of the Alexander polynomial of alternating links, see [St75].

1.10 Knot tables

For some time I have been interested in using knot tables, compiled by Hoste, Thistlethwaite, and Weeks, to seek knots with interesting properties, and so to provide examples and counterexamples to problems that have remained inaccessible using (entirely) manual reasoning (see e.g. [St33]).

1.11 Other topics

I have also done some work on unknotting numbers [St22], link polynomials [St43], number theoretic properties of knot invariants [St23, St24], enumeration problems of links [SV, St53], and everywhere equivalent links [St77, St78, St79].

2 Present and future Research

Knot theory attracts with a variety of problems, many of which are easy to formulate but nonetheless difficult to resolve. One such outstanding problem, around since the origin of knot tables by Tait and Little at the end of the 19th century, is the additivity of the crossing number under connected sum.

I will list now some main topics of research I was interested in at various points. My choice of problems is not fixed, and will also depend on my interaction with other mathematicians. Thus priorities shift with the time, and the below selection is not uniformly relevant (and neither is it complete), but it will outline some main directions of work in the visible future. At every topic I will also briefly explain the expected results of its investigation.

2.1 Hyperbolic volume

There have been so far several situations, in which the hyperbolic volume exhibits a relation to a combinatorily defined knot invariant. The most important one is Kashaev's conjecture on values of colored Jones polynomials, popularized by H. Murakami.

Another correspondence was observed by Brittenham, namely that the volume is bounded on alternating knots of given genus. His bound can be improved by inequalities of Lackenby-Agol-Thurston involving an invariant of knot diagrams called twist number. These bounds are also related to conjectures of Dunfield, namely that the volume linearly approximates a logarithm of the determinant of alternating knots. I'm currently interested in obtaining and improving such inequalities.

2.2 Trivalent graphs and enumeration of knots by genus

There is also a relation between the Brittenham approach and the enumeration problems of knots of given genus, and the sl_N weight system of trivalent graphs known from the theory of Vassiliev invariants.

One can express the maximal volume of knots of given canonical genus by links L_G associated to planar trivalent graphs G similarly to Habiro's claspers. The sl_N weight system of G then is related to both the hyperbolic volume and the enumeration of knots by genus, and also to the enumeration of 1-vertex triangulations of oriented surfaces carried out by my collaborator A. Vdovina.

2.3 Weight system-volume-conjectures

The form of the relation between the sl_N weight system W_N of G and volume of L_G is not yet clear, but calculations suggest that definitely something is going on beyond accidental coincidences. (A brief outline of this phenomenon can be found in the last section of my book [St91], as well as in the preparatory article [St76].) I hope in the future to deepen my understanding of hyperbolic volumes, in particular to understand better these relations. I hope also to find out whether and what is a relation of these coincidences to the Volume conjecture. For example, can one calculate the colored Jones polynomials of L_G , and establish the relation modulo the Volume conjecture? Can one gain insight into the Volume conjecture from these relations? This is also linked to understanding the, in particular multiplicative, structure of the sl_N weight systems of G. Few facts are known, including the multiplicative character of Vogel's algebra and Bar-Natan's version of the 4-Color-Theorem. A new observation from the work of Bacher and Vdovina on 1-vertex triangulations is that the linear term of the sl_N weight systems vanishes in Euler characteristic < -1. Their work also implies bounds on the number of linear monomials in the calculation of W_N , that in turn bound the asymptotical growth of the number of alternating knots of given genus, which I seek to improve. I hope to progress on at least some of these many interrelated problems in the future.

2.4 Non-trivial Jones polynomial problem

I seek further generalizations of the non-triviality result for the Jones polynomial, for example to arborescent knots. I also try to prove that there are achiral knots of any odd crossing number at least 15.

2.5 Braids

I'm also working on some problems of braids, for example the question of Rudolph whether (strongly) quasipositive knots have (strongly) quasipositive braid representations of minimal strand number. I expect counterexamples but they are not easy to construct. (I had in the past some counterexamples for positive braid representations and, jointly with M. Hirasawa, minimal genus band representations [HS].)

With R. Shinjo, we prove that under fairly general conditions an iterated exchange move, as introduced by Birman and Menasco, gives infinitely many non-conjugate braid representatives. As a consequence, every knot has infinitely many conjugacy classes of *n*-braid representatives if and only if it has one admitting an exchange move. This work is related in result to [St72], but the approach is entirely different. We are finalizing a paper on this topic, and seek in how far one can generalize this statement to links.

2.6 Number theoretic properties of knot invariants

One of my original mathematical interests was number theory (my specialization turned into a different direction by the influence I experienced during my studies). I'm interested in situations in which knot invariants can be studied from the point of view of some elementary number theoretic properties. A series of problems I intend to work on is related to determinants of achiral knots with particular properties, for example unknotting number one. These determinants are sums of two squares. It would be interesting to study which such numbers occur in which situations. Number theoretic properties of the determinant have also applications to unknotting numbers and knot distance, and maybe I can find more such applications.

2.7 Gauss sum invariants

There are still opportunities left in the application of Gauss sum invariants to positive knots and related knot classes, most naturally, to improve the existing inequalities. More importantly, there is a (long-term and long-postponed) computational project is to implement some of Fiedler's new character Gauss sum invariants (which take as input not a single diagram, but a sequence of diagrams of knots in the solid torus), and see what they distinguish. Ideally, one hopes to distinguish knot orientation with them, after the success on braids. This will obviously give a huge impetus on the theory of Gauss sum invariants.

2.8 Arc index and maximal Thurston- Bennequin invariant

Recently, I am working on using knot polynomial invariants to determine the arc index and maximal Thurston-Bennequin invariant of many knots.

2.9 Other topics

Much progress remains to be done on Hoste's conjecture, notably the proof even for simple classes like 2-bridge links, alternating 3-braid links, etc.

There is a conjectured classification of everywhere equivalent links [St77], and it would be interesting to verify its completeness in special cases. This was done for 3-braids in [St78] and 2 components in [St79]. The 3-component case at least looks feasible.

Extending work of Ishiwata, I determined the 5-move equivalence classes of Montesinos links up to mutation; one obtains from this a Jones and Kauffman polynomial test for a Montesinos link [St58]. A minor problem has remained to remove 'up to mutation'. A 5-move preserves the 5-Burnside group of the link group, and maps 1-to-1 the homomorphisms to a fixed 5-group, so I may explore group theoretic ways to accomplish this.